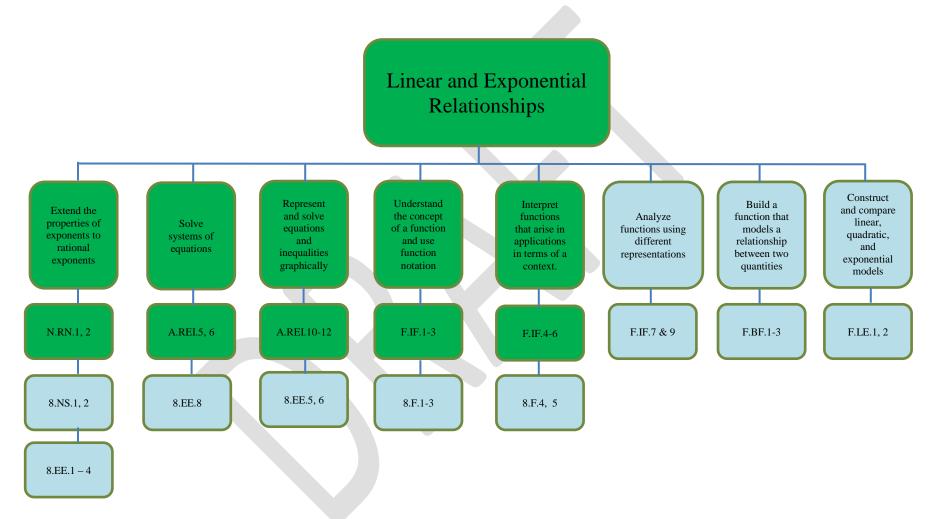
Los Angeles Unified School District Alternative Accelerated CC Math 8/ Algebra 1

Unit 2



GRADE 7 Super Accelerated – UNIT 2 Linear and Exponential Relationships

Critical Area: Students will learn function notation and develop the concepts of domain and range. They move beyond viewing functions as processes that take inputs and yield outputs and start viewing functions as objects in their own right. They explore many examples of functions, including sequences; they interpret functions given graphically, numerically, symbolically, and verbally, translate between representations, and understand the limitations of various representations. They work with functions given by graphs and tables, keeping in mind that, depending upon the context, these representations are likely to be approximate and incomplete. Their work includes functions that can be described or approximated by formulas as well as those that cannot. When functions describe relationships between quantities arising from a context, students reason with the units in which those quantities are measured. Students explore systems of equations and inequalities, and they find and interpret their solutions. Students build on and informally extend their understanding of integer exponents to consider exponential functions. They compare and contrast linear and exponential functions, distinguishing between additive and multiplicative change. They interpret arithmetic sequences as linear functions and geometric sequences as exponential functions.

Rationale- The study of functions requires students to use graphs, tables, sequences and formulas. In addition students must be able to represent functions numerically and symbolically. This requires students to have an understanding of the number system, specifically rational and irrational numbers involving square and cube roots. Furthermore, student must be able to represent and calculate expressions with exponents. Therefore, this unit on functions combines relevant grade 8 standards involving exponents, square and cube roots, expressions and equations. The purpose of this combination of standards is to give students the ability to have a complete understanding of the concept of functions.

CLUSTERS	COMMON CORE STATE STANDARDS	
Know that there are numbers that are not	8.NS.1 . Know that numbers that are not rational are called irrational. Understand informally that every	
rational, and approximate them by rational	number has a decimal expansion; for rational numbers show that the decimal expansion repeats eventually,	
numbers.	and convert a decimal expansion which repeats eventually into a rational number.	
	8.NS.2. Use rational approximations of irrational numbers to compare the size of irrational numbers, locate	
	them approximately on a number line diagram, and estimate the value of expressions (e.g.,). For example,	
	by truncating the decimal expansion of $\sqrt{\ }$, show that $\sqrt{\ }$ is between 1 and 2, then between 1.4 and 1.5, and	
	explain how to continue on to get better approximations.	
Work with radicals and integer exponents.	8.EE.1 Know and apply the properties of integer exponents to generate equivalent numerical expressions.	
	For example, $3^2 \times 3^{-5} = 3^{-3} = 1/3^3 = 1/27$.	
	8.EE.2 Use square root and cube root symbols to represent solutions to equations of the form $x^2 = p$ and $x^3 = 1$	
	p, where p is a positive rational number. Evaluate square roots of small perfect squares and cube roots of	
	small perfect cubes. Know that $\sqrt{2}$ is irrational.	
	8.EE.3 Use numbers expressed in the form of a single digit times an integer power of 10 to estimate very	
	large or very small quantities, and to express how many times as much one is than the other. For example,	

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Extend the properties of exponents to rational exponents.	estimate the population of the United States as 3×10^8 and the population of the world as 7×10^9 , and determine that the world population is more than 20 times larger. 8.EE.4 Perform operations with numbers expressed in scientific notation, including problems where both decimal and scientific notation are used. Use scientific notation and choose units of appropriate size for measurements of very large or very small quantities (e.g., use millimeters per year for seafloor spreading). Interpret scientific notation that has been generated by technology. N.RN.1. Explain how the definition of the meaning of rational exponents follows from extending the properties of integer exponents to those values, allowing for a notation for radicals in terms of rational exponents. For example, we define 51/3 to be the cube root of 5 because we want $(51/3)3 = 5(1/3)3$ to hold, so $(51/3)3$ must equal 5.
Analyze and solve linear equations and pairs of simultaneous linear equations	 N.RN.2 Rewrite expressions involving radicals and rational exponents using the properties of exponents. 8.EE.8 Analyze and solve pairs of simultaneous linear equations a. Understand that solutions to a system of two linear equations in two variables correspond to points of intersection of their graphs, because points of intersection satisfy both equations simultaneously. b. Solve systems of two linear equations in two variables algebraically, and estimate solutions by graphing the equations. Solve simple cases by inspection. For example, 3x + 2y = 5 and 3x + 2y = 6 have no solution because 3x + 2y cannot simultaneously be 5 and 6. c. Solve real-world and mathematical problems leading to linear equations in two variables. For example, given coordinates for two pairs of points, determine whether the line through the first pair of points intersects the line through the second pair.
Solve systems of equations. Linear-linear and linear-quadratic.	A.REI.5 . Prove that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions A.REI.6 . Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables.
Represent and solve equations and inequalities Graphically. Linear and exponential; learn as general principle.	A.REI.10. Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane, often forming a curve (which could be a line). A.REI.11. Explain why the x-coordinates of the points where the graphs of the equations $y=f(x)$ and $y=g(x)$ intersect are the solutions of the equation $f(x) = g(x)$ find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where $f(x)$ and/or $g(x)$ are linear, polynomial, rational, absolute value, exponential, and logarithmic functions. A.REI.12. Graph the solutions to a linear inequality in two variables as a half-plane (excluding the boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half-planes.
Define evaluate and compare functions	8.F.1. Understand that a function is a rule that assigns to each input exactly one output. The graph of a function is the set of ordered pairs consisting of an input and the corresponding output.

Understand the connections between	 8.F.2 Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). For example, given a linear function represented by a table of values and a linear function represented by an algebraic expression, determine which function has the greater rate of change. 8.F.3 Interpret the equation y = mx + b as defining a linear function, whose graph is a straight line; give examples of functions that are not linear. For example, the function A = s2 giving the area of a square as a function of its side length is not linear because its graph contains the points (1,1), (2,4) and (3,9), which are not on a straight line. 8.EE.5 Graph proportional relationships, interpreting the unit rate as the slope of the graph. Compare two
proportional relationships, lines and linear	different proportional relationships represented in different ways. For example, compare a distance-time
equations.	graph to a distance-time equation to determine which of two moving objects has greater speed. 8.EE.6 Use similar triangles to explain why the slope m is the same between any two distinct points on a non-vertical line in the coordinate plane; derive the equation $y = mx$ for a line through the origin and the equation $y = mx + b$ for a line intercepting the vertical axis at b .
Understand the concept of a function and use function notation.	F-IF.1 Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If f is a function and x is an element of its domain, then $f(x)$ denotes the output of f corresponding to the input x . The graph of f is the graph of the equation $y = f(x)$. F-IF.2 Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. F-IF.3 Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of the integers. For example, the Fibonacci sequence is defined recursively by $f(0) = f(1) = 1$, $f(n + 1) = f(n) + f(n - 1)$ for n 1.
Build a function that models a relationship	F.BF.1. Write a function that describes a relationship between two quantities.
between two quantities.	a. Determine an explicit expression, a recursive process, or steps for calculation from a context.
Limit to F.BF.1a, 1b, and 2 to linear and	b. Combine standard function types using arithmetic operations. For example, build a function that models
exponential functions. In F.BF.2, connect	the temperature of a cooling body by adding a constant function to a decaying exponential, and relate these
arithmetic sequences to linear functions and	functions to the model.
geometric sequences to exponential functions.	F.BF.2. Write arithmetic and geometric sequences both recursively and with an explicit formula, use them to model situations, and translate between the two forms.
Build new functions from existing functions.	F.BF.3. Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$, $k f(x)$, $f(kx)$, and $f(x + k)$ for specific
Focus on vertical translations of graphs of linear	values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and
and exponential functions. Relate the vertical	illustrate an explanation of the effects on the graph using technology. <i>Include recognizing even and odd</i>
translation of a linear function to its y-intercept.	functions from their graphs and algebraic expressions for them.
While applying other transformations to a linear	
graph is appropriate at this level, it may be difficult	
for students to identify or distinguish between the	

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effects of the other transformations included in this standard.		
Construct and compare linear, quadratic, and	F.LE.1 . Distinguish between situations that can be modeled with linear functions and with exponential	
exponential models	functions. a. Prove that linear functions grow by equal differences over equal intervals, and that exponential functions	
	grow by equal factors over equal intervals.	
	b. Recognize situations in which one quantity changes at a constant rate per unit interval relative to another.	
	c. Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval	
	relative to another.	
	F.LE.2 . Construct linear and exponential functions, including arithmetic and geometric sequences, given a	
	graph, a description of a relationship, or two input-output pairs (include reading these from a table).	
Use functions to model relationships between	8.F.4 Construct a function to model a linear relationship between two quantities. Determine the rate of	
quantities	change and initial value of the function from a description of a relationship or from two (x, y) values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear	
	function in terms of the situation it models, and in terms of its graph or a table of values.	
	8.F.5 Describe qualitatively the functional relationship between two quantities by analyzing a graph (e.g.,	
	where the function is increasing or decreasing, linear or nonlinear). Sketch a graph that exhibits the	
	qualitative features of a function that has been described verbally.	
Interpret functions that arise in applications in	F.IF.4 For a function that models a relationship between two quantities, interpret key features of graphs and	
terms of a context.	tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the	
Focus linear and exponential functions	relationship. Key features include: intercepts; intervals where the function is increasing, decreasing,	
	positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.	
	F.IF.5 Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. For example, if the function h gives the number of person-hours it takes to assemble n engines in	
	a factory, then the positive integers would be an appropriate domain for the function.	
	F.IF.6 Calculate and interpret the average rate of change of a function (presented symbolically or as a table)	
	over a specified interval. Estimate the rate of change from a graph.	
Analyze functions using different	F.IF.7. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases	
representations.	and using technology for more complicated cases.	
Linear, exponential, quadratic, absolute value, step,	a. Graph linear and quadratic functions and show intercepts, maxima, and minima.	
piecewise-defined.	b. Graph square root, cube root, and piecewise-defined functions, including step functions and absolute	
	value functions.	
	F.IF.9 . Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). For example, given a graph of one quadratic function and	
	an algebraic expression for another, say which has the larger maximum.	
MATHEMATICS PRACTICES		
1. Make sense of problems and persevere in	As you begin the year, it is advised that you start with MP1, MP3 and MP4 to set up your expectations of	
solving them.	your classroom. This will help you and your students become proficient in the use of these practices. All	

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- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the arguments of others.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.

other practices may be evident based on tasks and classroom activities.

LEARNING PROGRESSIONS

CDE Progress to Algebra K-8 www.cde.ca.gov/be/cc/cd/documents/updateditem12catt3.doc

Progression on HS Math - http://commoncoretools.me/wp-content/uploads/2012/12/ccss_progression_functions_2012_12_04.pdf

Interactive Wire Diagram for prerequisite standards http://www.curtiscenter.math.ucla.edu/MapApp/prg map.html

ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	KEY VOCABULARY
 Write in equivalent forms that represent both linear and exponential functions and construct functions to describe the situation and to find solutions Apply rules that builds a function that models a relationship between two quantities Represent equations and inequalities in one variable in various ways and use them to extend the properties of exponents to rational exponents Understand the relationship between quantities of two systems of equations and the methods to solve two system of linear equations Model with linear and exponential functions. 	 Why is it important to identify and extend the properties of exponents to rational exponents? When do students decide which is the best method to solve an inequality? How do you know which method to use in solving a system of equations? Why is it important to analyze functions using different representations? How do I analyze algebraic equations/inequalities to solve problems? What must students understand in order to create equations that describe numbers or relationships? How do students know which is the most efficient ways to build a function 	Explicit Function Geometric Sequence In-equalities Linear Range Rate of change Rational Recursively Symmetries

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rce/attachments/algebra-i-m1-copy-ready-materials.pdf face after they have worked with basic exponential functions like these. Illustrative Mathematics Skeleton Tower – F. BF.1a http://www.illustrativemathematics.org/illustrations/ns/75 A Sum of Functions – F. BF. 1a face after they have worked with basic exponential functions like these. Example. On June 1, a fast growing species of algae is accidentally introduced into a lake in a city park. It starts to grow and cover the surface of the lake in such a way that the area covered by A Sum of Functions – F. BF. 1a face after they have worked with basic exponential functions like these. Lample. On June 1, a fast growing species of algae is accidentally introduced into a lake in a city park. It starts to grow and cover the surface of the lake in such a way that the area covered by Cellular growth: F-LE.2 and F-BF.2	RESOURCES	that models a relationship between two quantities? • Why is it important to understand solving a system of linear and exponential relationships in two variables algebraically and graphically? • Is there functional relationship in non-linear and ambiguous data? INSTRUCTIONAL STRATEGIES	ASSESSMENT
ns/230 Lake Algae – F. BF.1a http://www.illustrativemathematics.org/illustrations/804 Logistic Growth Model, Explicit Version: F-IF.4 http://www.insidemathematics.org/illustrations/804 Lnside Mathematics http://www.insidemathematics.org/index.php/tools-forteachers/ course-1-algebra Tools for algebra grow unabated, the lake will be totally covered and the fish in the lake will suffocate. At the rate it is growing this will happen on June 30. a. When will the lake be covered halfway? b. Write an equation that represents the percentage of the surface area of the lake that is covered in algae as a function of time (in days) that passes since the algae was introduced into the lake. Facilitate a discussion that would direct students to generate recursive formula for the	California Revised Mathematics Framework: http://www.cde.ca.gov/be/cc/cd/draftmathfwchap ters.asp. Engage New York http://www.engageny.org/sites/default/files/resou rce/attachments/algebra-i-m1-copy-ready- materials.pdf Illustrative Mathematics Skeleton Tower – F. BF.1a http://www.illustrativemathematics.org/illustratio ns/75 A Sum of Functions – F. BF. 1a http://www.illustrativemathematics.org/illustratio ns/230 Lake Algae – F. BF.1a http://www.illustrativemathematics.org/illustratio ns/533 Logistic Growth Model, Explicit Version: F-IF.4 http://www.illustrativemathematics.org/illustratio ns/804 Inside Mathematics http://www.insidemathematics.org/index.php/too ls-forteachers/	Exponential Growth. When a quantity grows with time by a multiplicative factor greater than 1, it is said the quantity grows exponentially. The following example illustrates the type of problem that students can face after they have worked with basic exponential functions like these. Example. On June 1, a fast growing species of algae is accidentally introduced into a lake in a city park. It starts to grow and cover the surface of the lake in such a way that the area covered by the algae doubles every day. If it continues to grow unabated, the lake will be totally covered and the fish in the lake will suffocate. At the rate it is growing this will happen on June 30. a. When will the lake be covered halfway? b. Write an equation that represents the percentage of the surface area of the lake that is covered in algae as a function of time (in days) that passes since the algae was introduced into the lake. Facilitate a discussion that would direct	PARCC - http://parcconline.org/samples/mathematics/high- schoolfunctions F-IF.9 http://parcconline.org/sites/parcc/files/PARCC_SampleItems _Mathematics_HSAlgIMylaPool_081913_Final.pdf Myla's Swimming Pool: F-LE.2 http://parcconline.org/sites/parcc/files/HSAlg1Math2MiniG olfPrices.pdf Mini -Golf Prices: F-BF.2 http://www.ccsstoolbox.com/parcc/PARCCPrototype_main. html

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http://map.mathshell.org/materials/lessons.php?ta skid=55 4#task554 Manipulating Radicals: N-RN http://map.mathshell.org/materials/lessons.php?ta skid=54 7#task547	n-1 for the following example: Populations of bacteria can double every 6 hours under ideal conditions, at least until the nutrients in its supporting culture are depleted. This means a population of 500 such bacteria would grow to 1000, etc. Use of Exit Slips to assess student understanding. http://daretodifferentiate.wikispaces.com/Pr e-Assessment EPR) strategies for whole group instruction.				
	Strategies to check for understanding:				
	Individual White Boards, Fist of Five, Exit				
Slip, etc.					
LANGUAGE GOALS					
Students will be able to justify (orally and in writing) their rationale for solving a system of equations using various methods.					
Example: To solve these equations, I use instead of because					
Students will be able to explain (writing/speaking/listening) their understanding of the properties of the quantity represented in terms of their context. Example: 3x - 9y = 5 and y = 1/3 x + 1					
Example: $3x - 9y = 3$ and $y = 1/3x + 1$. Students will be able to read a word problem and identify the language need to create an algebraic representation.					
Students will be able to explain (orally and in writing) and justify their rationale for their choice of method to solve inequality equations.					
Example: To solve this inequality, I use because					
Students will be able to describe their understanding (orally and in writing) math vocabulary around whole expressions and equations.					
PERFORMANCE TASKS					
Illustrative Mathematic Influenza epidemic: F.IF.4 http://www.illustrativemathematics.org/illustrations/637 Logistic Growth Model, Abstract Version: F.IF.4 http://www.illustrativemathematics.org/illustrations/800 How is the Weather?: F.IF.4 http://www.illustrativemathematics.org/illustrations/649 Telling a Story With Graphs: F.IF.4 http://www.illustrativemathematics.org/illustrations/650 LAUSD Concept Lessons – http://math.lausd.net/middle-school/algebra-1-concept-lessons Tying the Knots Mathematics Assessment Project Formative Assessments/ Tasks Comparing Investment – F.LE 1-5. http://map.mathshell.org/materials/download.php?fileid=1250 Fuctions and Everyday – F.BF.1 and F.LE.1-5: http://map.mathshell.org/materials/download.php?fileid=1259					

DIFFERENTIATION		
FRONT LOADING	ACCELERATION	INTERVENTION
• Students apply their understanding of the properties of	• Students will design a word problem that reflects the	Use real-word context examples to
exponents.	use of graphing inequalities.	demonstrate the meaning of the parts of a
• Students apply and extend their knowledge of rational	• Students will write a scenario and explain the	system of equations for the students.
numbers to exponents and to find the values of	process needed to solve a system of linear equations	• Use of visual interactive websites that
numerical values that include those numbers.	with two variables.	through the manipulation of graphs represent
• Students apply their knowledge about the meaning of	Have student create a real world problem where	inequalities.
the representation of radicals with rational exponents.	students will	• Students find it useful through technology to
• Students will understand that if the two sides of one	build a function that model a relationship between two	recognize function that represent the same
equation are equal, and the two sides of another equation	quantities.	relationship.
are equal, then the sum (or difference) of these is equal.	• Have students apply their math knowledge that will	Provide a situation that uses realia to
• Students will extend their knowledge of learning the	extend the properties of exponents to exponential	demonstrate how to build a function that
relationship between the algebraic representation and its	functions.	model a relationship between two quantities.
graph.	• Students will compare and contrast the properties of	
• Students will use their prior knowledge of creating	a linear equation and linear inequality equation.	
tables of values for function to find a solution.		
• Students will extend their prior knowledge of graphing		
two equations and be able to interpret the intersection of		
the graph as the solution to the original equation.		

¹ Major Clusters – area of intensive focus where students need fluent understanding and application of the core concepts.

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- 6. Partnership for Assessment of Readiness for College and Career. (2012). PARCC Assessments. Retrieved from http://www.parcconline.org/parcc-assessment.

² Supporting/Additional Clusters – designed to support and strengthen areas of major emphasis/expose students to other subjects.

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